Chapter 13
Return, Risk, and the Security Market Line

Key Concepts and Skills
• Know how to calculate expected returns
• Understand the impact of diversification
• Understand the systematic risk principle
• Understand the security market line
• Understand the risk-return trade-off
• Be able to use the Capital Asset Pricing Model

Chapter Outline
• Expected Returns and Variances
• Portfolios
• Announcements, Surprises, and Expected Returns
• Risk: Systematic and Unsystematic
• Diversification and Portfolio Risk
• Systematic Risk and Beta
• The Security Market Line
• The SML and the Cost of Capital: A Preview
Expected Returns

- Expected returns are based on the probabilities of possible outcomes
- In this context, “expected” means average if the process is repeated many times
- The “expected” return does not even have to be a possible return

\[ E(R) = \sum_{i=1}^{n} p_i R_i \]

- Use this for returns, and portfolio betas

Portfolio Expected Returns

- The expected return of a portfolio is the weighted average of the expected returns of the respective assets in the portfolio

\[ E(R_p) = \sum_{j=1}^{m} w_j E(R_j) \]

- You can also find the expected return by finding the portfolio return in each possible state and computing the expected value as we did with individual securities

Variance and Standard Deviation

- Variance and standard deviation measure the volatility of returns
- Using unequal probabilities for the entire range of possibilities
- Weighted average of squared deviations

\[ \sigma^2 = \sum_{i=1}^{n} p_i (R_i - E(R))^2 \]
Portfolio Variance

- Compute the portfolio return for each state:
  \[ R_p = w_1R_1 + w_2R_2 + \ldots + w_mR_m \]
- Compute the expected portfolio return using the same formula as for an individual asset
- Compute the portfolio variance and standard deviation using the same formulas as for an individual asset

Efficient Markets

- Efficient markets are a result of investors trading on the unexpected portion of announcements
- The easier it is to trade on surprises, the more efficient markets should be
- Efficient markets involve random price changes because we cannot predict surprises

Total Risk

- Total risk = systematic risk + unsystematic risk
- The standard deviation of returns is a measure of total risk
- For well-diversified portfolios, unsystematic risk is very small
- Consequently, the total risk for a diversified portfolio is essentially equivalent to the systematic risk
Systematic Risk

- Risk factors that affect a large number of assets
- Also known as non-diversifiable risk or market risk
- Includes such things as changes in GDP, inflation, interest rates, etc.

Table 13.7

<table>
<thead>
<tr>
<th>(1) Number of Stocks in Portfolio</th>
<th>(2) Average Annual Portfolio Returns</th>
<th>(3) Ratio of Portfolio Standard Deviation to Standard Deviation of a Single Stock</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10.24</td>
<td>12.60</td>
</tr>
<tr>
<td>2</td>
<td>17.26</td>
<td>16.76</td>
</tr>
<tr>
<td>4</td>
<td>20.80</td>
<td>20.54</td>
</tr>
<tr>
<td>8</td>
<td>24.90</td>
<td>24.01</td>
</tr>
<tr>
<td>16</td>
<td>29.00</td>
<td>29.63</td>
</tr>
<tr>
<td>32</td>
<td>33.00</td>
<td>32.84</td>
</tr>
<tr>
<td>64</td>
<td>37.00</td>
<td>36.87</td>
</tr>
<tr>
<td>128</td>
<td>41.00</td>
<td>40.92</td>
</tr>
<tr>
<td>256</td>
<td>45.00</td>
<td>44.00</td>
</tr>
<tr>
<td>512</td>
<td>49.00</td>
<td>48.00</td>
</tr>
<tr>
<td>1,024</td>
<td>53.00</td>
<td>52.12</td>
</tr>
</tbody>
</table>


Figure 13.1

A graph showing the relationship between the number of stocks in a portfolio and the average annual portfolio returns, illustrating the reduction in non-diversifiable risk as the number of stocks increases.
Measuring Systematic Risk

- How do we measure systematic risk?
  - We use the beta coefficient.
- What does beta tell us?
  - A beta of 1 implies the asset has the same systematic risk as the overall market.
  - A beta < 1 implies the asset has less systematic risk than the overall market.
  - A beta > 1 implies the asset has more systematic risk than the overall market.

The Capital Asset Pricing Model (CAPM)

- The capital asset pricing model defines the relationship between risk and return.
  - \( E(R_A) = R_f + \beta_A (E(R_M) - R_f) \)
- If we know an asset's systematic risk, we can use the CAPM to determine its expected return.
- This is true whether we are talking about financial assets or physical assets.

Factors Affecting Expected Return

- Pure time value of money: measured by the risk-free rate.
- Reward for bearing systematic risk: measured by the market risk premium.
- Amount of systematic risk: measured by beta.
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Expected Returns

- Expected returns are based on the probabilities of possible outcomes
- In this context, “expected” means average if the process is repeated many times
- The “expected” return does not even have to be a possible return

\[
E(R) = \sum_{i=1}^{n} p_i R_i
\]

- Use this for returns, and portfolio betas

Example: Expected Returns

- Suppose you have predicted the following returns for stocks C and T in three possible states of the economy. What are the expected returns?

<table>
<thead>
<tr>
<th>State</th>
<th>Probability</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>Boom</td>
<td>0.3</td>
<td>15</td>
</tr>
<tr>
<td>Normal</td>
<td>0.5</td>
<td>10</td>
</tr>
<tr>
<td>Recession</td>
<td>0.2</td>
<td>2</td>
</tr>
</tbody>
</table>

- \( R_C = 0.3(15) + 0.5(10) + 0.2(2) = 9.9\% \)
- \( R_T = 0.3(25) + 0.5(20) + 0.2(1) = 17.7\% \)
Variance and Standard Deviation

- Variance and standard deviation measure the volatility of returns.
- Using unequal probabilities for the entire range of possibilities.
- Weighted average of squared deviations.

\[ \sigma^2 = \sum\limits_{i=1}^{n} p_i (R_i - E(R))^2 \]

Example: Variance and Standard Deviation

- Consider the previous example. What are the variance and standard deviation for each stock?
- Stock C
  \[ \sigma^2 = .3(15-9.9)^2 + .5(10-9.9)^2 + .2(2-9.9)^2 = 20.29 \]
  \[ \sigma = 4.50\% \]
- Stock T
  \[ \sigma^2 = .3(25-17.7)^2 + .5(20-17.7)^2 + .2(1-17.7)^2 = 74.41 \]
  \[ \sigma = 8.63\% \]

Another Example

- Consider the following information:

<table>
<thead>
<tr>
<th>State</th>
<th>Probability</th>
<th>ABC, Inc. (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Boom</td>
<td>.25</td>
<td>15</td>
</tr>
<tr>
<td>Normal</td>
<td>.50</td>
<td>8</td>
</tr>
<tr>
<td>Slowdown</td>
<td>.15</td>
<td>4</td>
</tr>
<tr>
<td>Recession</td>
<td>.10</td>
<td>-3</td>
</tr>
</tbody>
</table>

- What is the expected return?
- What is the variance?
- What is the standard deviation?
Portfolios

• A portfolio is a collection of assets
• An asset’s risk and return are important in how they affect the risk and return of the portfolio
• The risk-return trade-off for a portfolio is measured by the portfolio expected return and standard deviation, just as with individual assets

Example: Portfolio Weights

• Suppose you have $15,000 to invest and you have purchased securities in the following amounts. What are your portfolio weights in each security?
  - $2000 of C
  - $3000 of KO
  - $4000 of INTC
  - $6000 of BP

  C: 2/15 = .133
  KO: 3/15 = .2
  INTC: 4/15 = .267
  BP: 6/15 = .4

Portfolio Expected Returns

• The expected return of a portfolio is the weighted average of the expected returns of the respective assets in the portfolio

\[ E(R_p) = \sum_{j=1}^{n} w_j E(R_j) \]

• You can also find the expected return by finding the portfolio return in each possible state and computing the expected value as we did with individual securities
Example: Expected Portfolio Returns

- Consider the portfolio weights computed previously. If the individual stocks have the following expected returns, what is the expected return for the portfolio?
  - C: 19.69%
  - KO: 5.25%
  - INTC: 16.65%
  - BP: 18.24%
  - \[ E(R_P) = 0.133(19.69) + 0.2(5.25) + 0.267(16.65) + 0.4(18.24) = 15.41\% \]

Portfolio Variance

- Compute the portfolio return for each state:
  \[ R_P = w_1R_1 + w_2R_2 + \ldots + w_mR_m \]
- Compute the expected portfolio return using the same formula as for an individual asset
- Compute the portfolio variance and standard deviation using the same formulas as for an individual asset

Example: Portfolio Variance

- Consider the following information
  - Invest 50% of your money in Asset A
  - State Probability A B Portfolio
    - Boom .4 30% -5% 12.5%
    - Bust .6 -10% 25% 7.5%
  - What are the expected return and standard deviation for each asset?
  - What are the expected return and standard deviation for the portfolio?
Another Example

• Consider the following information

<table>
<thead>
<tr>
<th>State</th>
<th>Probability</th>
<th>X</th>
<th>Z</th>
</tr>
</thead>
<tbody>
<tr>
<td>Boom</td>
<td>.25</td>
<td>15%</td>
<td>10%</td>
</tr>
<tr>
<td>Normal</td>
<td>.60</td>
<td>10%</td>
<td>9%</td>
</tr>
<tr>
<td>Recession</td>
<td>.15</td>
<td>5%</td>
<td>10%</td>
</tr>
</tbody>
</table>

• What are the expected return and standard deviation for a portfolio with an investment of $6,000 in asset X and $4,000 in asset Z?

Expected vs. Unexpected Returns

• Realized returns are generally not equal to expected returns
• There is the expected component and the unexpected component
  • At any point in time, the unexpected return can be either positive or negative
  • Over time, the average of the unexpected component is zero

Announcements and News

• Announcements and news contain both an expected component and a surprise component
• It is the surprise component that affects a stock’s price and therefore its return
• This is very obvious when we watch how stock prices move when an unexpected announcement is made or earnings are different than anticipated
**Efficient Markets**

- Efficient markets are a result of investors trading on the unexpected portion of announcements
- The easier it is to trade on surprises, the more efficient markets should be
- Efficient markets involve random price changes because we cannot predict surprises

**Systematic Risk**

- Risk factors that affect a large number of assets
- Also known as non-diversifiable risk or market risk
- Includes such things as changes in GDP, inflation, interest rates, etc.

**Unsystematic Risk**

- Risk factors that affect a limited number of assets
- Also known as unique risk and asset-specific risk
- Includes such things as labor strikes, part shortages, etc.
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Returns

• Total Return = expected return + unexpected return
• Unexpected return = systematic portion + unsystematic portion
• Therefore, total return can be expressed as follows:
  • Total Return = expected return + systematic portion + unsystematic portion

Diversification

• Portfolio diversification is the investment in several different asset classes or sectors
• Diversification is not just holding a lot of assets
• For example, if you own 50 Internet stocks, you are not diversified
• However, if you own 50 stocks that span 20 different industries, then you are diversified
The Principle of Diversification

- Diversification can substantially reduce the variability of returns without an equivalent reduction in expected returns.
- This reduction in risk arises because worse than expected returns from one asset are offset by better than expected returns from another.
- However, there is a minimum level of risk that cannot be diversified away and that is the systematic portion.

### Table 13.7

<table>
<thead>
<tr>
<th>Number of stocks</th>
<th>Average standard deviation</th>
<th>Standard deviation of returns</th>
<th>Ratio of portfolio standard deviation to standard deviation of any single stock</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.24</td>
<td>0.60</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>0.27</td>
<td>0.76</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>0.29</td>
<td>0.80</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>0.30</td>
<td>0.81</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>0.31</td>
<td>0.83</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>0.33</td>
<td>0.85</td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>0.37</td>
<td>0.91</td>
<td></td>
</tr>
<tr>
<td>50</td>
<td>0.42</td>
<td>0.97</td>
<td></td>
</tr>
<tr>
<td>100</td>
<td>0.50</td>
<td>1.00</td>
<td></td>
</tr>
<tr>
<td>200</td>
<td>0.53</td>
<td>1.03</td>
<td></td>
</tr>
<tr>
<td>500</td>
<td>0.57</td>
<td>1.07</td>
<td></td>
</tr>
<tr>
<td>1,000</td>
<td>0.61</td>
<td>1.10</td>
<td></td>
</tr>
</tbody>
</table>

*Note: Values are from Table 13.6. See also, "How Many Stocks Make a Diversified Portfolio?" Journal of Financial and Quantitative Analysis, 27 (September 1992), pp. 535-553. The data were derived from J. C. Heaton and H. W. Zhang, "Diversification and Portfolio Size: An Inflation Bias?" Journal of Business 65 (December 1992), pp. 409-437.*
**Diversifiable Risk**

- The risk that can be eliminated by combining assets into a portfolio
- Often considered the same as unsystematic, unique or asset-specific risk
- If we hold only one asset, or assets in the same industry, then we are exposing ourselves to risk that we could diversify away

**Total Risk**

- Total risk = systematic risk + unsystematic risk
- The standard deviation of returns is a measure of total risk
- For well-diversified portfolios, unsystematic risk is very small
- Consequently, the total risk for a diversified portfolio is essentially equivalent to the systematic risk

**Systematic Risk Principle**

- There is a reward for bearing risk
- There is not a reward for bearing risk unnecessarily
- The expected return on a risky asset depends only on that asset's systematic risk since unsystematic risk can be diversified away
Measuring Systematic Risk

- How do we measure systematic risk?
  - We use the beta coefficient.
- What does beta tell us?
  - A beta of 1 implies the asset has the same systematic risk as the overall market.
  - A beta < 1 implies the asset has less systematic risk than the overall market.
  - A beta > 1 implies the asset has more systematic risk than the overall market.

Table 13.8 – Selected Betas

<table>
<thead>
<tr>
<th>Security</th>
<th>Beta Coefficient</th>
<th>Standard Deviation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kroger Co.</td>
<td>0.95</td>
<td>20%</td>
</tr>
<tr>
<td>Coca-Cola</td>
<td>1.25</td>
<td>30%</td>
</tr>
<tr>
<td>NV</td>
<td>1.50</td>
<td>20%</td>
</tr>
<tr>
<td>Microsoft</td>
<td>1.50</td>
<td>30%</td>
</tr>
<tr>
<td>Google</td>
<td>1.50</td>
<td>20%</td>
</tr>
<tr>
<td>eBay</td>
<td>1.50</td>
<td>30%</td>
</tr>
<tr>
<td>A barricade &amp; Fitch</td>
<td>1.50</td>
<td>20%</td>
</tr>
<tr>
<td>Bank Of America, Inc.</td>
<td>1.50</td>
<td>30%</td>
</tr>
</tbody>
</table>

Total vs. Systematic Risk

- Consider the following information:

<table>
<thead>
<tr>
<th>Security</th>
<th>Standard Deviation</th>
<th>Beta</th>
</tr>
</thead>
<tbody>
<tr>
<td>Security C</td>
<td>20%</td>
<td>1.25</td>
</tr>
<tr>
<td>Security K</td>
<td>30%</td>
<td>0.95</td>
</tr>
</tbody>
</table>

- Which security has more total risk?
- Which security has more systematic risk?
- Which security should have the higher expected return?
Work the Web Example

- Many sites provide betas for companies
- Yahoo Finance provides beta, plus a lot of other information under its Key Statistics link
- Click on the web surfer to go to Yahoo Finance
  - Enter a ticker symbol and get a basic quote
  - Click on Key Statistics

Example: Portfolio Betas

- Consider the previous example with the following four securities

<table>
<thead>
<tr>
<th>Security</th>
<th>Weight</th>
<th>Beta</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>.133</td>
<td>2.685</td>
</tr>
<tr>
<td>KO</td>
<td>.2</td>
<td>0.195</td>
</tr>
<tr>
<td>INTC</td>
<td>.267</td>
<td>2.161</td>
</tr>
<tr>
<td>BP</td>
<td>.4</td>
<td>2.434</td>
</tr>
</tbody>
</table>

- What is the portfolio beta?
- \[ .133(2.685) + .2(0.195) + .267(2.161) + .4(2.434) = 1.947 \]

Beta and the Risk Premium

- Remember that the risk premium = expected return – risk-free rate
- The higher the beta, the greater the risk premium should be
- Can we define the relationship between the risk premium and beta so that we can estimate the expected return?
  - YES!
Example: Portfolio Expected Returns and Betas

Reward-to-Risk Ratio: Definition and Example

- The reward-to-risk ratio is the slope of the line illustrated in the previous example
  - Slope = \( \frac{E(R_A) - R_f}{\beta_A} \)
  - Reward-to-risk ratio for previous example = \( \frac{20 - 8}{1.6 - 0} = 7.5 \)
- What if an asset has a reward-to-risk ratio of 8 (implying that the asset plots above the line)?
- What if an asset has a reward-to-risk ratio of 7 (implying that the asset plots below the line)?

Market Equilibrium

- In equilibrium, all assets and portfolios must have the same reward-to-risk ratio, and they all must equal the reward-to-risk ratio for the market
  \[
  \frac{E(R_A) - R_f}{\beta_A} = \frac{E(R_M - R_f)}{\beta_M}
  \]
Security Market Line

- The security market line (SML) is the representation of market equilibrium
- The slope of the SML is the reward-to-risk ratio: \((E(R_m) - R_f) / \beta_m\)
- But since the beta for the market is always equal to one, the slope can be rewritten
- Slope = \(E(R_m) - R_f\) = market risk premium

The Capital Asset Pricing Model (CAPM)

- The capital asset pricing model defines the relationship between risk and return
- \(E(R_A) = R_f + \beta_A(E(R_m) - R_f)\)
- If we know an asset’s systematic risk, we can use the CAPM to determine its expected return
- This is true whether we are talking about financial assets or physical assets

Factors Affecting Expected Return

- Pure time value of money: measured by the risk-free rate
- Reward for bearing systematic risk: measured by the market risk premium
- Amount of systematic risk: measured by beta
Example - CAPM

Consider the betas for each of the assets given earlier. If the risk-free rate is 4.15% and the market risk premium is 8.5%, what is the expected return for each?

<table>
<thead>
<tr>
<th>Security</th>
<th>Beta</th>
<th>Expected Return</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>2.685</td>
<td>4.15 + 2.685(8.5) = 26.97%</td>
</tr>
<tr>
<td>KO</td>
<td>0.195</td>
<td>4.15 + 0.195(8.5) = 5.81%</td>
</tr>
<tr>
<td>INTC</td>
<td>2.161</td>
<td>4.15 + 2.161(8.5) = 22.52%</td>
</tr>
<tr>
<td>BP</td>
<td>2.434</td>
<td>4.15 + 2.434(8.5) = 24.84%</td>
</tr>
</tbody>
</table>

Figure 13.4

Quick Quiz

- How do you compute the expected return and standard deviation for an individual asset? For a portfolio?
- What is the difference between systematic and unsystematic risk?
- What type of risk is relevant for determining the expected return?
- Consider an asset with a beta of 1.2, a risk-free rate of 5%, and a market return of 13%
  - What is the reward-to-risk ratio in equilibrium?
  - What is the expected return on the asset?
Comprehensive Problem

• The risk free rate is 4%, and the required return on the market is 12%. What is the required return on an asset with a beta of 1.5?
• What is the reward/risk ratio?
• What is the required return on a portfolio consisting of 40% of the asset above and the rest in an asset with an average amount of systematic risk?

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